## Accounting for Job-to-Job Moves: Wages Versus Values

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## Motivation

- Job-to-job transitions are an important part of labor reallocation
- $60 \%$ of new hires come directly from other jobs
- 10\% of workers each year make an EE transition
- Moving jobs is a common way of obtaining earnings increases
- Yet there appears to be a substantial amount of wage cuts
- Wage cuts are not necessarily puzzling from a dynamic perspective if they are associated with increases in value
- Key question: are these wage cuts associated with positive or negative changes in value?
- Important for understanding efficiency of the labor market, risk over the life cycle, policy design
- Motivations for switching jobs affect the allocation of workers to firms and determine which features should be included in models
- Link between labor market fluidity and welfare


## Motivations for Wage and Value Changes

- Wage
+ Wage
+ Value
- Value

Accept wage cut now in exchange for future wage growth: Postel-Vinay and Robin (2002)

Non-wage amenities, forced moves: Sorkin (2018), Hall and Mueller (2018), Moscarini and (2012), Luo and Mongey (2019) Postel-Vinay (2019)

Good move for both immediate wages and future wages

Borrowing constraints: Lise

| Accept wage cut now in ex- <br> change for future wage growth: <br> Postel-Vinay and Robin (2002) | Good move for both immediate <br> wages and future wages |
| :--- | :--- |
|  |  |
| Non-wage amenities, forced <br> moves: Sorkin (2018), Hall and | Borrowing constraints: Lise <br> Mueller (2018), Moscarini and <br> (2012), Luo and Mongey (2019) |

## What We Do

1. Refine measurement of job-to-job transitions

- Made possible by high frequency administrative data from Denmark
- Precise pinpointing of transition and clear wage measures

2. Compute wage change CDFs for stayers and switchers
3. Semi-parametric estimation of value of a job for a worker

- Nest value functions in commonly used search models

4. Analyze the joint distribution of wage changes and value changes for job-to-job transitions

- With model, we assign a change in value associated with every wage change we observe
- Quantify value cuts, toward an understanding of who is taking them and why


## Preview of Results

## Measurement

- About half of job-to-job transitions feature a wage cut, but only a quarter of these are more than 10\%
- But it makes a difference how you measure these!


## Wages vs. values

- Changes in value are typically smaller in magnitude than wage changes
- $60 \%$ of wage cuts also feature declines in value
- Motivations for EE switches tend to be related to unobservable match + job characteristics
- Lots of variation as to whether future wages or future transitions are quantitatively responsible for the value changes


## OUtLINE

Measurement and Motivating Facts

Model of Job Values

Results

## Measurement and Motivating

FACTS

## DATA

Danish administrative registry data

- Entire Danish population from 2008 to 2017
- Monthly payroll records reported by employers
- Total pay each month, firm ID, contractual hours, occupation, industry, demographics,...
- Public transfers database for unemployment and OLF states

What is a job?

- Firm $\times 2$-digit occupation
- Why? Wages in same firm differ across occupation, relevant for model
- Cells under 1000 person-quarter observations are grouped by 4 -digit industry $\times$ 2-digit occupation

Quarterly aggregation to keep model tractable, but still can track moves through U

## Distribution of Wage Growth



## How to Measure Wages

Construct measure of base real wage

- Issue: spikes during the last month, representing payouts from holiday fund
- Drop last wage observation + calculate 12-month centered moving average

Sample: full-time workers who are attached to the labor force

- Only consider jobs with contractual hours within $2 \%$ of 160 hours per month (full-time)
- Ensures measured wage change during job switch not driven by hours


## Wage Growth for Switchers: Alternate Measurements

|  | Decrease > 10\% | Increase > 10\% |
| :--- | :---: | :---: |
| Baseline | 0.13 | 0.14 |
| Fail to drop last wage obs. | 0.19 | 0.14 |
| Looser hours restriction | 0.17 | 0.18 |
| Previous two combined | 0.26 | 0.16 |

- Our adjustments reduce the noise present in the original data
- Careful measurement matters, especially at the tails

Model of Job Values

## Objectives

- Want to translate our wage changes into value changes
- PDV of future wages in a job consists of:

1. Wage stream in that job
2. Transition rates to other jobs

- Need a model for

1. Predicting wages for any worker in any job
2. Predicting transitions between jobs for any worker

- Approach

1. Define worker and job types
2. Define state variables
3. Estimate wage and transition as function of state variables by type

- How to pick state variables? Guided by theory. Today: a variant of the wage posting model of Burdett and Mortensen (1998)


## Environment

## Workers

- Workers can be one of $i \in I$ types (will drop $i$ subscripts)
- Type-specific component of earnings: g
- Live from $a=1,2, \ldots, A$
- Age profile of earnings differs across types: h(a)

Jobs

- Workers transition between J jobs
- This set also includes non-employment states
- Piece-rate in each job: $\omega(j)$

Wages: $\omega(j) h(a) g z$

- z: match-specific productivity


## Environment

## Matches

- When matched to a job, workers have a match-specific productivity z
- Helps match the wage changes of job switchers
- After moving $j \rightarrow k$, draw new $z^{\prime}$ from a distribution that depends on $(j, k, z)$
- $z^{\prime}$ revealed if the match is created
- Allow for persistence in $z$ when workers switch between jobs
- Productivity in new job may depend on the identity of the old job
- Stayers' wages are subject to i.i.d. mean 0 shocks $\varepsilon$
- Helps match stayers' wage growth
- Contact rate from job $j$ to $k: \lambda_{k}(a, j, z)$
- Workers may be more likely to leave lower-paying jobs or jobs at which they're not productive


## Value Function

$$
\begin{aligned}
v(a, j, z) & =\overbrace{\omega(j) h(a) g z}^{\text {today's wages }} \\
& +\beta[\sum_{k} \underbrace{\lambda_{k}(a, j, z) \mathbb{I}_{\{d(a, j, k, z)=1\}} \mathbb{E}_{z \times \varepsilon} \vee\left(a+1, k, z^{\prime} \varepsilon^{\prime}\right)}_{\text {expected value of switching from job } j \text { to job } k}+\underbrace{\Lambda(a, j, z) \mathbb{E}_{\varepsilon} v\left(a+1, j, z \varepsilon^{\prime}\right)}_{\text {expected value of staying at job } j}]
\end{aligned}
$$

- Burdett-Mortensen: constant job-specific wage piece rate, probability of moving to other jobs depends on current job, no renegotiation in response to outside offers
- Generalizations: life-cycle, match-specific productivity, i.i.d. shocks to stayers' wages
- Instead of computing equilibria of structural model, calculate ingredients needed to solve for $v(a, j, z)$


## IMPLEMENTATION

Ingredients: $\omega(j), h(a), g, z, \lambda_{k}(a, j, z)$, expectations over $z^{\prime}$ for switchers

## Worker types

- Correspond to 4 fixed education $\times$ gender categories


## Job types $j$

- 6019 employment states (about half correspond to firm $\times$ occupation; other half corresponds to industry $\times$ occupation)
- 10 non-employment states: short- and long-term unemployment, retirement, maternity leave, sick leave, etc. that we observe transfers for

Age profile $h(a)$

- $w(j), z$ constant within match $\rightarrow$ average wage change between $a$ and $a+1$ for stayers
- Pool across jobs and over time, take cumulative sum of earnings changes


## WAGE PREMIA $\omega(j)$

Separate each component of earnings: $w_{n}(a, j, z)=\omega(j) h(a) g z$

- Selection issue: what if workers' mobility decisions are based on $z$ ?
- Averaging earnings within jobs and worker types would give biased estimates of $\omega(j)$
- Assumption: while unemployed, $z$ is low enough such that all workers accept any job offer $\Longrightarrow$ their distribution of $z$ is the same across jobs

With $g$ in hand, for jobs with enough hires from $U, \omega(j)$ is:

$$
\frac{1}{U_{j}} \sum_{n=1}^{U_{j}} \frac{w_{n}\left(a_{n}, j_{n}, z_{n}\right)}{h\left(a_{n}\right) g_{n}}=\frac{1}{U_{j}} \sum_{n=1}^{U_{j}} \frac{\omega(j) h(a) g \mathbb{E}[z]}{h(a) g}=\omega(j) \quad \forall n: j_{n}=j
$$

- Key: expectation over $z$ is the same as the unconditional, normalized to 1 for all $j$
- For jobs less workers hired from $U$, impute $\omega(j)$ via statistical methods


## MATCH-SPECIFIC PRODUCTIVITY

- Match-specific productivity $z_{n}$ in data:

$$
z_{n}=\frac{w_{n}\left(a_{n}, j_{n}, z_{n}\right)}{\omega\left(j_{n}\right) h\left(a_{n}\right) g_{n}}
$$

- Necessary step for computing values: law of motion for z'
- Want to generate accurate wage predictions at the individual level so we can trust value predictions!
- Model with and without $z$ fit the overall CDF of wage changes well
- For job switchers from $j$ to $k$, want to forecast $z^{\prime}$ as a function of the model's state variables: $z^{\prime}=f(a, j, k, z)$
- Specification that yields the best forecast is:

$$
\begin{aligned}
\log z_{i}^{\prime} & =\bar{z}+\rho \log z_{i}+\beta_{1} \log \omega_{i}+\beta_{2} \log \omega_{i}^{\prime}+\beta_{3} \operatorname{mean}\left(z \mid \omega_{i}\right)+\beta_{4} \operatorname{mean}\left(z \mid \omega_{i}^{\prime}\right) \\
& +\beta_{5} \operatorname{var}\left(z \mid \omega_{i}\right)+\beta_{6} \operatorname{var}\left(z \mid \omega_{i}^{\prime}\right)+\eta_{i}
\end{aligned}
$$

## eE Wage Change Predictions: Without Match-Specific Productivity

Wage Change Predictions


- On their own, piece rates do not do well at predicting individual wage changes


## EE Wage Change Predictions: With Match-Specific Productivity z

## Wage Change Predictions



- Incorporating z into the model helps to better match individual wage changes obenedz


## Everrthing else

- Transition probabilities: $\lambda_{k}(a, j, z)$
- Use observed transitions among the whole set of jobs in the data
- Workers at better paying jobs or with higher z may be less willing to leave
- Group a into 3 age bins and $z$ into 4 quartiles
- Distribution of $z$ for UE transitions
- Comes from variance of $z$ in the data for workers hired out of $U$
- Distribution of $\varepsilon$
- Comes directly from variance of wage changes for stayers


## Results

## Densities of Wage and Value Changes

Distributions of wage and value changes


- Value changes smaller in magnitude than wage changes Histograms


## Majority of Moves Result in Value Increase



- $\operatorname{Pr}($ value increase $\mid$ wage cut $)=39.6 \% ; \operatorname{Pr}($ value cut $\mid$ wage increase $)=23.8 \%$
- No major differences within fixed worker groups (gender $\times$ education) worter types


## Younger Workers Tend to Increase w; Older Workers Tend to Increase v






- Younger workers more likely borrowing constrained
- Older workers tend to take more wage cuts that result in higher values


## Better Matches Tend to Increase Both Wages and Value



4th quartile $z$ change


- Increasing z is likely to be good for both wages and values


## Still Lots of Wage Cuts for Moves to Higher-Paying Jobs

1st quartile piece rate change


4th quartile piece rate change


- In contrast to $z$, moving up in $\omega(j)$ is more closely tied to increases in value
- Piece rate $\neq$ wage $\neq$ value


## Transition Rates are an Important Component of Value

Ratio: wage component to transition component of value


- Decompose the change in value from $(j, z)$ to $\left(k, z^{\prime}\right)$ into 2 components, coming from wages and transition rates
- Value changes come from all different mixes


## Conclusion and Future Work

- Developed a methodology for assigning values associated with job-to-job transitions
- Findings
- Careful measurement for documenting features of EE switches
- Significant mass in all quadrants of wage change/value change plane
- Unobserved heterogeneity is key for determining values behind each switch
- Next steps

1. Better understand the motivations behind the transitions

- Recover distribution of non-wage amenities or reallocation shocks that rationalize negative value switches
- See if switches coincide with family events, geographic moves, changes in wealth or consumption, etc.

2. Further develop the model

- Allow for other forms of worker and job heterogeneity
- Extend to Postel-Vinay and Robin (2002) setting


## ReLATED Literature

Measurement

- Nominal wage changers for stayers: Grigsby, Hurst, Yildirmaz (2020)
- Wage changes using administrative data: Kurmann and McEntarfer (2018), Jardim et al. (2019)

Reasons for wage cuts

- Future wage growth, transitions to other jobs: Postel-Vinay and Robin (2002)
- Non-wage amenities: Sorkin (2018), Hall and Mueller (2018)
- "Godfather" shocks: Moscarini and Postel-Vinay (2019) and lots of others


## TYPE-SPECIFIC PREMIA $g(i)$

- Let $U_{i j}$ be the number of workers of type $i$ hired into job $j$ from unemployment
- For jobs with $U_{i j} \geq 25$, compute the following:

$$
\frac{1}{U_{i j}} \sum_{n=1}^{U_{i j}} \frac{w_{n}\left(a_{n}, j_{n}, z_{n}\right)}{h\left(a_{n}\right)}=\frac{1}{U_{i j}} \sum_{n=1}^{u_{i j}} \frac{\omega(j) h(a) g(i) \mathbb{E}[z]}{h(a)}=\omega(j) g(i) \quad \forall n: j_{n}=j
$$

- Key: expectation over $z$ is the same as the unconditional, assumed to be 1 for all $j$
- Set $g(i)=1$ for baseline group, weighted average of $g(i) \omega(j)$ over $j$, and compare to weighted average of $\omega(j)$ for baseline group


## WAGE PREMIA $\omega(j):$ FOR JOBS WITH FEWER OBSERVATIONS

1. For jobs with few observations, first compute naive $\tilde{\omega}(j)$ using all hires:

$$
\tilde{\omega}(j)=\frac{1}{N_{j}} \sum_{n=1}^{N_{j}} \frac{w_{n}\left(a_{n}, j_{n}, z_{n}\right)}{h\left(a_{n}\right) g_{n}}
$$

2. For jobs with $U_{j} \geq 10$ estimate the following:

$$
\log \omega(j)=\beta_{0}+\beta_{1} \log \tilde{\omega}(j)+\beta_{2} X_{j}+\epsilon_{j}
$$

$X_{j}$ contains firm size, occupation, industry
3. Use this relationship to impute a $\omega(j)$ for jobs with less than 10 hires from unemployment

## Relationship Between $\omega(j)$ AND $\tilde{\omega}(j)$



## ee Wage Change Predictions: With Observed Match-Specific Productivity z



## Densities of Wage and Value Changes

Distribution of wage changes


Distribution of value changes


## EDUCATION $\times$ GENDER

Female + College
Male + College





## Tenure



## Firm and Occupation Switches



Back

## INITIAL WAGE




## INItIAL PIECE RATE

1st quartile initial piece rate


4th quartile initial piece rate


## INITIAL Z



## DECOMPOSITION BY QUADRANT

Decrease Wage + Increase Value
Increase Wage + Increase Value


